

p. 137 (19) A particle moves along a line so that its position at any time  $t \geq 0$  is given by the function  $s(t) = t^2 - 3t + 2$  where  $s$  is measured in meters and  $t$  is measured in seconds.

a) Find the displacement during the first 5 seconds.

$$\Delta y \text{ or } \Delta s$$

b) Find the average velocity during the first 5 seconds.

Slope

c) Find the instantaneous velocity when  $t = 4$ .

$$s'(t)$$

d) Find the acceleration of the particle when  $t = 4$ .

$$s''(t) = v'(t)$$

e) At what values of  $t$  does the particle change direction?

$$v(t) = 0$$

$$2t - 3 = 0$$

$$t = \frac{3}{2} \text{ sec}$$

f) Describe the particles motion

$$(0, \frac{3}{2})$$

$$v(1) = -1 < 0$$

moving left/down

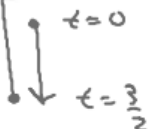
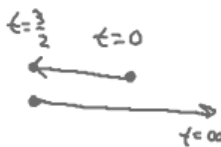
$$(\frac{3}{2}, \infty)$$

$$v(2) = 1 > 0$$

moving right/up

$$s(t) = t^2 - 3t + 2$$

$$v(t) = 2t - 3$$



a) Find the body's velocity, speed, and acceleration at time  $t$ .

b) Find the the body's velocity, speed, and acceleration at time  $t = \frac{\pi}{4}$

position

Part a

15.  $s(t) = 2\sin t + 3\cos t$

$$v(t) = 2\cos t - 3\sin t$$

$$a(t) = -2\sin t - 3\cos t$$

$$\begin{aligned}\text{speed} &= |v(t)| \\ &= |2\cos t - 3\sin t|\end{aligned}$$

Part B

$$\begin{aligned}v(\pi/4) &= 2\cos \pi/4 - 3\sin \pi/4 \\ &= 2\left(\frac{\sqrt{2}}{2}\right) - 3\left(\frac{\sqrt{2}}{2}\right)\end{aligned}$$

$$\begin{aligned}a(\pi/4) &= -2\sin(\pi/4) - 3\cos(\pi/4) \\ &= -2\left(\frac{\sqrt{2}}{2}\right) - 3\left(\frac{\sqrt{2}}{2}\right)\end{aligned}$$

$$\text{speed} = \left| \frac{2\sqrt{2}}{2} - \frac{3\sqrt{2}}{2} \right|$$